MHF 4UI Unit #3 – Exponential and Logarithmic Functions – Exam Review

1. Evaluate. If possible, state exact answers. Otherwise, round to two decimals.

a)
$$\log_3(81)$$
 b) $\log_6(1)$ c) $\log_5\left(\frac{1}{125}\right)$ d) $\log(1000)$

e)
$$\log_2(24) - \log_2\left(\frac{3}{2}\right)$$
 f) $\log_6(4) + \log_6(9)$ g) $\log_6\left(\frac{1}{216}\right)$ h) $\log_2(1024)$

2. Solve. If possible, state exact answers. Otherwise, round to four decimals.

a)	$7(2)^{-x} = 5^{2x+3}$	b)	$3(4)^x = 13^{3x-1}$
c)	$-9e^{8x-5}+7=-20$	d)	$\log(x) = 2\log(3) + 3\log(2)$
e)	$\log_4(x+2) - \log_4(x-3) = \log_4(9)$	f)	$6e^{4x+3}-5=13$
g)	$\log_4(x+2) + \log_4(x-1) = 1$	h)	$\log_3(8x+7) + \log_3(x+1) = 2$
i)	$\ln\left(x^2-9\right)=1$	j)	$e^x = 5$
k)	$\ln(5x-2) = 7$	I)	$e^{\frac{x}{3}} = 2e$

- 3. A plug-in air freshener loses about 4% of its scent every 3 days. Find the number of days until the freshener only has 25% of its original scent. (Round your answer to the nearest day.)
- 4. The half-life of Cesium-144 is 282 days. How long is it until only 10% remains? (Round your answer to the nearest day.)
- 5. A collector comic book, currently worth \$40, is predicted to grow in value 15%/a.
 - a) How much is this book predicted to be worth in 10 years?
 - b) How long would you have to wait for this book to double in value?
- 6. On each bounce a ball rises 70% of the height from which it fell. Let us agree that, for all practical purposes, the ball stops bouncing when the height to which it rises is only 0.1% of the height from which it was dropped originally. How many bounces will this take?

Answers:

1.	a) 4	b) 0	c) –3	d) 3	e) 4	f) 2	g) –3	h) 10
2.	a) –0.7368	b) 0.5807	c) 0.7623	d) 72	e) $\frac{29}{8}$	f) –.4753	g) 2	h) 1/8
	i) $\pm \sqrt{e+9}$	j) ln(5)	k) $\frac{e^7+2}{5}$	l) $3\ln(2e)$				
3.	102 days							
4.	937 days							

- 5. a) \$161.82 b) 5 years
- 6. 20 bounces