

U3D8_T Combining Transformations

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U3D8_T
Combinin...

U3D8

Warm Up:

Describe the transformations that have occurred to $h(x)$ to obtain the function $y = -5h\left(\frac{2}{3}x\right)$

1. reflection in x -axis
 2. vertical stretch factor 5
 3. Horizontal stretch factor 1.5
- reciprocal of $\frac{2}{3}$ is $\frac{3}{2}$ or 1.5
- $-5 \times y$
- $1.5 \times x$

If $(-1, 4)$ is a point on the function $h(x)$, what would be the new point on the transformed function?

$$(x, y) \rightarrow (1.5x, -5y)$$

$$(-1, 4) \rightarrow (1.5(-1), -5(4))$$

$$(-1, 4) \rightarrow (-1.5, -20)$$

$(-1, 4)$ reflected in x -axis becomes $(-1, -4)$
 $(-1, -4)$ with vertical stretch factor 5 becomes $(-1, -20)$
 $(-1, -20)$ with horizontal stretch factor $\frac{3}{2}$ becomes $(-1.5, -20)$

Combining Transformations

When a function has a combination of transformations, apply them in order left to right when in the form:

$$y = \pm af[\pm b(x - h)] + k$$

Diagram illustrating the order of transformations for the function $y = \pm af[\pm b(x - h)] + k$:

- reflect. in x-axis** (Red arrow pointing to the first \pm)
- vert. Stretch/comp.** (Blue arrow pointing to a)
- reflect in y-axis** (Green arrow pointing to the second \pm)
- horizontal Stretch/Compression ($\frac{1}{b}$)** (Black arrow pointing to b)
- shift Left/Right** (Red arrow pointing to the third \pm)
- shift up/down** (Blue arrow pointing to k)

- ① Reflection in x-axis with Vertical Stretches and Compressions.
- ② Reflection in y-axis with Horizontal Stretches and Compressions.
- ③ Translations (Horizontal and Vertical Shifts)

Example 1:

a) Describe, in order, how the graph of $y = -2f(4(x - 2))$ can be obtained from the graph of $y = f(x)$.

1. reflection in x -axis

2. vertical stretch factor 2 } $-2 \times y$ multiply by $\frac{1}{2}$

3. Horizontal Compression factor $\frac{1}{4}$
 (or horizontal compression by 4) } $\frac{1}{4}x + 2$
 "divide by 4"

4. Shift right 2.

b) If (x, y) was a point on $f(x)$, what would the value of the coordinates be after the 4 transformations?

$(x, y) \rightarrow (\frac{1}{4}x + 2, -2y)$

⊙ $(\frac{x}{4} + 2, -2y)$

the word compression is most important. A compression factor 4 means you are dividing by 4 but if you say compression factor $\frac{1}{4}$, it means you are multiplying by $\frac{1}{4}$ both give same result.

Our textbook interchanges these ...
 Some textbooks consistently do it one way or the other
 As long as I see the word compression, I am not concerned whether you write $\frac{1}{4}$ or 4.

Example 2:

Given $f(x) = x^2 + 3$

a) Describe how the graph of $y = -\frac{1}{2}f(2x+6) - 2$ can be obtained from $f(x)$.

*First factor out the coefficient on x if $b \neq 1$ and $h \neq 0$.

$$y = -\frac{1}{2} f[2(x+3)] - 2$$

1. reflect in x -axis.
2. vert. comp. factor $\frac{1}{2}$
3. Hor. Comp. factor $\frac{1}{2}$

4. Shift left 3
5. Shift down 2

b) What is the new "image equation"?

$$y = -\frac{1}{2} f[2(x+3)] - 2$$

$$f(x) = x^2 + 3$$

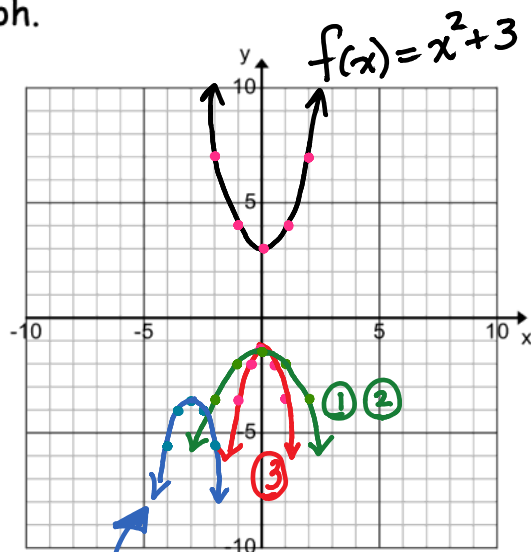
$$y = -\frac{1}{2} [(2[x+3])^2 + 3] - 2$$

$$y = -\frac{1}{2} [(2)^2(x+3)^2 + 3] - 2$$

$$y = -\frac{1}{2} (4)(x+3)^2 - \frac{3}{2} - \frac{4}{2}$$

$$y = -2(x+3)^2 - \frac{7}{2}$$

c) Graph.



$$y = -\frac{1}{2} f[2(x+3)] - 2$$

$$y = -2(x+3)^2 - \frac{7}{2} \quad V(-3, -3.5)$$

U3D8 Practice: p. 240 #7(odd), 8-9(odd, sketch one from each), 14