U7D4 MCR 3UI

Arithmetic Series

An arithmetic series is the ______ of the terms of an arithmetic sequence.

If the sequence is $t_1, t_2, t_3, t_4, \dots, t_n$, then the series is $S_1, S_2, S_3, S_4, \dots, S_n$ where :

$$s_{1} = t_{1}$$

$$s_{2} = t_{1} + t_{2}$$

$$s_{3} = t_{1} + t_{2} + t_{3}$$

$$s_{4} = t_{1} + t_{2} + t_{3} + t_{4}$$

. . .

In general,

$$s_{n} = \frac{n}{2} [2a + (n-1)d]$$

a is
d is
n is

Or the formula can be written as :

$$s_{n} = \frac{n}{2} [2a + (n-1)d]$$

$$s_{n} = \frac{n}{2} [a + a + (n-1)d]$$

$$s_{n} = \frac{n}{2} [t_{1} + t_{n}]$$

$$s_{n} = n \left[\frac{t_{1} + t_{n}}{2}\right]$$

And so, we have two different versions of the same formula.

Examples:

- 1. Find the sum of the first 100 terms of $8 + 11 + 14 + \ldots$
- 2. Find the sum of 1.1 + 1.2 + 1.3 + 1.4 + . . . + 8.9
- 3. If the sum of n terms of a sequence is given by $S_n = n^2 + n$, find t_{11} .

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