

U7D2_T Arithmetic Sequences

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8:29 PM



U7D2_T
Arithmeti...

Warm Up.

a) $8, 12, 16, \dots$

$$t_n = 4n + 4$$

b) $-4, -1, 4, 11, \dots$

$$t_n = n^2 - 5$$

c) $10, 50, 250, 1250, \dots$

$$t_n = 2(5)^n$$

U7D2

Arithmetic Sequences

What is similar about the following sequences?

1. $3, 5, 7, 9, 11$

$\swarrow \quad \swarrow \quad \swarrow \quad \swarrow$
 $2 \quad 2 \quad 2 \quad 2$

2. $-1, 4, 9, 14, 19$

$\swarrow \quad \swarrow \quad \swarrow \quad \swarrow$
 $5 \quad 5 \quad 5 \quad 5$

3. $20, 17, 14, 11, 8$

$\swarrow \quad \swarrow \quad \swarrow \quad \swarrow$
 $-3 \quad -3 \quad -3 \quad -3$

All are
linear
(First differences
are constant).

All of these sequences are classified as **arithmetic** sequences since each term is generated by adding a **COMMON DIFFERENCE** or **d** to the previous term. The first term is designated as **a** .

An arithmetic sequence looks like :

$a, a + d, a + 2d, a + 3d, a + 4d, \dots$ or

In general,

$$t_n = a + (n - 1)d$$

note: $a - d$ is the y-int of a linear graph

t_n = the 'general term'
or the n^{th} term

a = the first term (t_1)

n = the term number
or the number of terms

d = the common difference
(This is the same as the first
difference column value; it
is the slope of the linear
function.)

Examples:

1. Determine t_n and t_{50} for the following arithmetic sequences:

a) $2, 6, 10, 14, \dots$

$a = 2 \quad d = 4$

$t_{50} = 4(50) - 2$

$t_n = a + (n - 1)d$

$t_{50} = 198$

$t_n = 2 + (n - 1)(4)$

$t_n = 2 + 4n - 4$

$t_n = 4n - 2$

b) $10, \frac{19}{2}, 9, \frac{17}{2}, \dots$ (Determine t_n and t_{50})

$$a=10 \quad d=-\frac{1}{2}$$

$$t_{50} = \frac{21-50}{2}$$

$$t_n = 10 + (n-1)\left(-\frac{1}{2}\right)$$

$$t_{50} = -\frac{29}{2}$$

$$t_n = 10 - \frac{1}{2}n + \frac{1}{2}$$

$$t_n = -\frac{1}{2}n + \frac{21}{2}$$

or

$$t_n = \frac{21-n}{2}$$

2. Determine the number of terms in the sequence 3, 7, 11, 15 199.

$$a=3 \quad d=4 \quad n=? \quad t_n=199$$

$$a + (n-1)d = t_n$$

$$3 + (n-1)(4) = 199$$

$$(n-1)4 = 196$$

$$n-1 = 49$$

$$n = 50$$

\therefore there are
50 terms in this
finite sequence.

3. Determine t_{50} if $t_4 = 5$ and $t_{11} = 26$ for an arithmetic sequence.

$(4, 5)$ $(11, 26)$ Using Gr. 9 math

$$d = \frac{26-5}{11-4} = \frac{21}{7} = 3$$

$$t_n = a + (n-1)d$$

$$5 = a + (4-1)(3)$$

$$5 = a + 9$$

$$a = -4$$

$$t_n = a + (n-1)d$$

$$t_{50} = -4 + 49(3)$$

$$t_{50} = 143$$

$$t_n = 3n - 7$$

Using Gr. 10 math:

$$a + (n-1)d = t_n$$

sub $d=3$ into ②

$$\textcircled{1} a + 10d = 26$$

$$\textcircled{2} a + 3d = 5$$

$$\begin{array}{r} a + 10d = 26 \\ a + 3d = 5 \\ \hline 7d = 21 \\ d = 3 \end{array}$$

$$a + 3(3) = 5$$

$$a = -4$$

$$t_{50} = -4 + 49(3)$$

$$t_{50} = 143$$

4. Describe the arithmetic sequence
 $t_n = 3n - 2$ as a recursive sequence.

1, 4, 7, ...

$$t_k = t_{k-1} + 3, t_1 = 1$$

↑
to find any term

take the term before it

and add 3.

beginning with the first term equal to one.

note: t_{k-1} is one term before t_k
 since $k-1$ is one less than k

U7D2 Practice: p. 441 #1-8(eoo), 9, 10, 15, 23, **29**

NOTE: eoo means every other one in each question- a, c, e, etc.)