

# U6D4\_T\_Horz Stretch Trig

Thursday, May 2, 2019

6:48 PM



U6D4\_T\_H  
orz Stretc...

## U6D4 MCR 3UI      Horizontal Stretches of Periodic Functions

**Recall:** When a trig function was vertically stretched (or compressed), the key idea was the fact that the function's **AMPLITUDE** was altered. Notice that if a graph is stretched/compressed vertically, a measurement on the y-axis is changed.

So, if we stretch/compress a graph horizontally, a measurement on the x-axis is changed.

From the graph of a trig function, what is the key term measured on the x-axis? **the Period**

### **In general:**

Transformations that applied to  $f(x)$ , also apply to trig functions:

For functions in the form  $y = \sin kx$  or  $y = \cos kx$ ,

- If  $k > 1$ , the graphs are horizontally compressed by a factor of  $\frac{1}{k}$
- If  $0 < k < 1$ , the graphs are horizontally stretched by a factor of  $\frac{1}{k}$
- **Amplitude** is unchanged
- **Period** becomes  $\frac{360^\circ}{k} \Rightarrow k = \frac{360^\circ}{\text{Period}}$

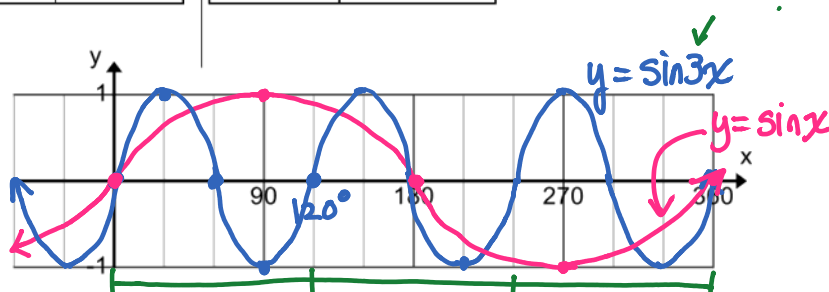
## Graphing Horizontal stretches/compressions using the 5-Point Graphing Method

When we have a horizontal stretch/compression, the period is altered, therefore our 5 key points will also be altered. Remember that the 5 key points divided our period into quarters...therefore, divide the new period by 4 and you will have the locations of the new 5 key points (the amplitude is unchanged, so our y-values will remain the same)

1. Graph  $y = \sin x$  and  $y = \sin 3x$  on the grid below.
- Recall the 5 Key Points of  $y = \sin x$
- horizontal compression factor  $\frac{1}{3}$   
 $\hookrightarrow k=3$   
 Period of  $y = \sin 3x$  is  $\frac{360^\circ}{3} = 120^\circ$   
 Therefore, our 5 key points will occur every  $30^\circ$ .

$x$	$\sin x$
$0^\circ$	0
$90^\circ$	1
$180^\circ$	0
$270^\circ$	-1
$360^\circ$	0

$x$	$\sin 3x$
$0^\circ$	0
$30^\circ$	1
$60^\circ$	0
$90^\circ$	-1
$120^\circ$	0



note: There are 3 complete cycles in  $360^\circ$   
 $k$  is always the number of complete cycles in  $360^\circ$ .

U6D4 Practice: Page 374 #2 (all – just in degrees, not radians), 3 – 6 (b only), 8b (typo – max is at 3), 10c, 11bc, 12c

Period =  $\frac{360^\circ}{k}$ ,  $k = \frac{1}{2}$

2. Graph  $y = \cos x$  and  $y = \cos \frac{1}{2}x$  on the grid below:

Period of  $y = \cos \frac{1}{2}x$  is:  $360^\circ \div \frac{1}{2}$ . Key points every  $\frac{720^\circ}{4} = 180^\circ$ .

$x$	$\cos x$
$0^\circ$	1
$90^\circ$	0
$180^\circ$	-1
$270^\circ$	0
$360^\circ$	1

$x$	$\cos \frac{1}{2}x$
$0^\circ$	1
$180^\circ$	0
$360^\circ$	-1
$540^\circ$	0
$720^\circ$	1

$= 360^\circ \times \frac{2}{1}$   
 $= 720^\circ$



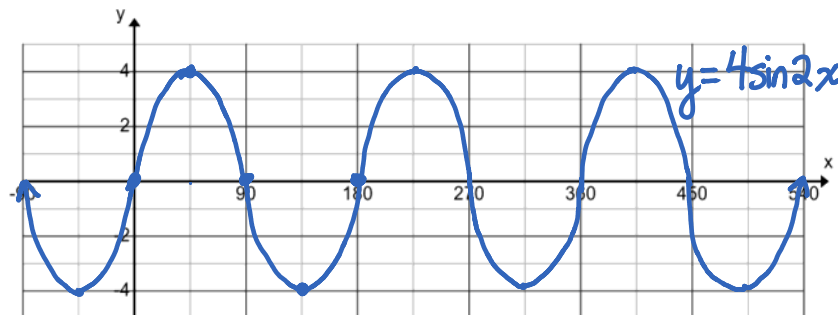
3. Graph  $y = 4 \sin 2x$  on the grid below

(graph the original function as well):

Amplitude: 4. Period: 180°.

Key points every: 45°.

$x$	$0^\circ$	$45^\circ$	$90^\circ$	$135^\circ$	$180^\circ$
$4 \sin 2x$	0	4	0	-4	0



$$k = \frac{360^\circ}{540^\circ} = \frac{2}{3}$$

4. A cosine function has an amplitude of 3 and a period of  $540^\circ$ .

a) Determine the equation of the function:  $y = 3\cos \frac{2}{3}x$

b) Sketch 2 cycles of this function, beginning with a point at  $x = 0$ .

Key points occur every:  $135^\circ$

$x$	$0^\circ$	$135^\circ$	$270^\circ$	$405^\circ$	$540^\circ$
$y$	3	0	-3	0	3

