c) $\frac{1}{1-\cos x} + \frac{1}{1+\cos x} = \frac{2}{\sin^2 x}$

INTRODUCTION TO TRIG IDENTITIES

 $\sin\theta =$



 $\cos\theta = \tan\theta =$

Example 1. Simplify (using terminal arm)

a). $\frac{\sin\theta}{\cos\theta}$

b). $sin^2\theta + cos^2\theta$

Proving Trigonometric Identities

Quotient Identity (QI):

Pythagorean Identity (PI):

In example 1, we discovered some trig "identities". They are called identities because they remain equal regardless of the value of θ . You have seen "identities" before; for example,

 $(x-5)(x+5) = x^2 - 25$ is considered an identity. If we are simplifying an expression, we can replace (x-5)(x+5) with $x^2 - 25$ or we could replace $x^2 - 25$ with (x-5)(x+5) without changing the value of the expression. We use identities to write an expression in a more convenient form.

Tips for Proving Trig Identities

1. Need to show the LS = RS by manipulating **<u>one side at a time only</u>**.

- (For grade 11 most of the proofs can be proven using one side of the expression only. In grade 12, you will usually need to work with both sides.)
- 2. Keep LS separate from RS at all times. NEVER 'move' anything from one side to the other (like you do when solving equations)!
- 3. Start by trying to work with the most complicated looking side first.
- 4. Remember you can manipulate the identities just like regular algebraic equations...

$$sin^2\theta + cos^2\theta = 1 \implies sin^2\theta = 1 - cos^2\theta \implies cos^2\theta = 1 - sin^2\theta$$

Any of these are called the Pythagorean Identity (PI).

5. May need to use a common denominator when adding or subtracting identities in fraction form. **Example 2**. Write an equivalent expression for:

a)
$$tanxcosx$$
 b) $sin^2\theta$ c) $\frac{1}{tan^2\theta}$

Example 3. Prove the following identities:

a)
$$\frac{\cos x \tan x}{\sin x} = 1$$
 b) $1 - \sin^2 \theta = \frac{\sin \theta \cos \theta}{\tan \theta}$

d) $\frac{\cos\theta}{1+\sin\theta} = \frac{1-\sin\theta}{\cos\theta}$ e) $\frac{\cos\theta}{1-\sin\theta} + \frac{\cos\theta}{1+\sin\theta} = \frac{2}{\cos\theta}$ Homework: p. 398 #1, 2bcgl, 4abei