

Unit 3 lesson 7

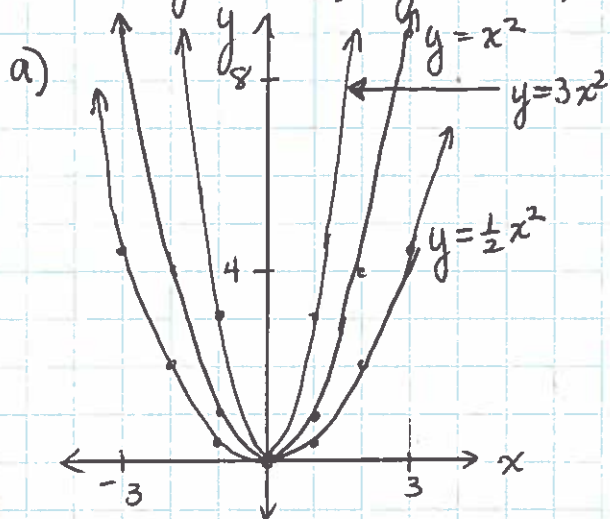
Pg 229 #3, 4ii, 5 eoo, 6 eoo, 7, 11 eoo

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3a)  $g(x) = 2f(x)$        $h(x) = 3f(x)$

b)  $g(x) = f(2x)$        $h(x) = f(\frac{1}{4}x)$

4 ii)  $y = x^2$ ,  $y = 3x^2$ ,  $y = \frac{1}{2}x^2$



b)  $y = 3x^2$  is a vertical stretch factor 3  
 $y = \frac{1}{2}x^2$  is a vertical compression factor  $\frac{1}{2}$ .

c) (0,0) is invariant

5 a)  $y = 3f(x)$       vertical stretch factor 3

b)  $y = \frac{1}{2}f(x)$       "      compression factor  $\frac{1}{2}$ .

c)  $y = 2f(x)$       "      stretch factor 2.

d)  $y = \frac{1}{3}f(x)$       "      compression factor  $\frac{1}{3}$ .

e)  $y = f(2x)$       horizontal compression factor  $\frac{1}{2}$  [or horizontal compression by 2]

f)  $y = f(\frac{1}{2}x)$       "      stretch      "      2

g)  $y = f(4x)$       "      compression      "       $\frac{1}{4}$ .

↳ (or horizontal compression by 4)

6a) transformation

a)  $y = 3f(2x)$       vertical stretch factor 3      horizontal compression factor  $\frac{1}{2}$  (OR HC by 2)

b)  $y = \frac{1}{2}f(\frac{1}{3}x)$       compression factor  $\frac{1}{2}$       stretch factor 3

c)  $y = 4f(\frac{1}{2}x)$       stretch factor 4      stretch factor 2

d)  $y = \frac{1}{3}f(3x)$       compression factor  $\frac{1}{3}$       compression factor  $\frac{1}{3}$  (OR HC by 3)

e)  $y = 2f(4x)$       stretch factor 2      compression factor  $\frac{1}{4}$  (OR HC by 4)

f)  $y = 5f(\frac{1}{2}x)$       "      "      5      stretch factor 2.

7a)  $y = x^2$  (red)

(blue)  
 $y = \frac{1}{2}f(x)$   
 $y = \frac{1}{2}x^2$

vertical compression factor  $\frac{1}{2}$

note error on scale in 7a graph

b)  $f(x) = x+1$

$y = 2f(x)$   
 $y = 2(x+1)$   
 $y = 2x+2$

vertical stretch factor 2

c)  $f(x) = \sqrt{x}$

$y = 2f(x)$   
 $y = 2\sqrt{x}$   
 new function

vertical stretch factor 2

11. transformation. (image equation)

Domain / Range

a)  $y = 3f(x)$

$y = 3\sqrt{16-x^2}$

$D = \{x \in \mathbb{R} \mid -4 \leq x \leq 4\}$   
 $R = \{y \in \mathbb{R} \mid 0 \leq y \leq 12\}$

c)  $y = f(2x)$

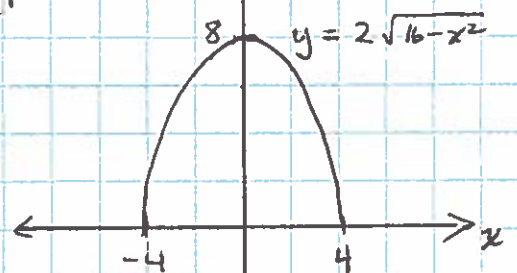
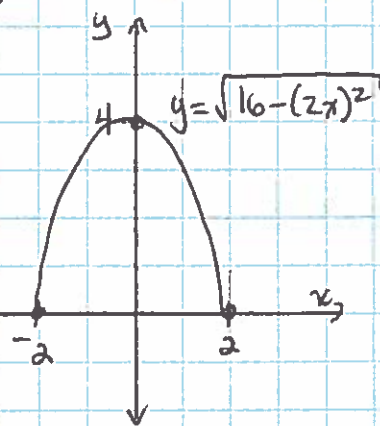
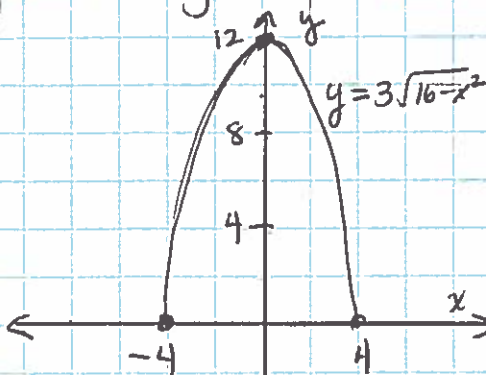
$y = \sqrt{16-(2x)^2}$

$D = \{x \in \mathbb{R} \mid -2 \leq x \leq 2\}$   
 $R = \{y \in \mathbb{R} \mid 0 \leq y \leq 4\}$

e)  $y = 2f(x)$

$y = 2\sqrt{16-x^2}$

$D = \{x \in \mathbb{R} \mid -4 \leq x \leq 4\}$   
 $R = \{y \in \mathbb{R} \mid 0 \leq y \leq 8\}$



b)  $y = \frac{1}{2}f(x)$

$y = \frac{1}{2}\sqrt{16-x^2}$

$D = \{x \in \mathbb{R} \mid -4 \leq x \leq 4\}$   $R = \{y \in \mathbb{R} \mid 0 \leq y \leq 2\}$

d)  $y = f(\frac{1}{2}x)$

$y = \sqrt{16-(\frac{1}{2}x)^2}$

$D = \{x \in \mathbb{R} \mid -8 \leq x \leq 8\}$   $R = \{y \in \mathbb{R} \mid 0 \leq y \leq 4\}$

e)  $y = f(4x)$

$y = \sqrt{16-(4x)^2}$

$D = \{x \in \mathbb{R} \mid -1 \leq x \leq 1\}$   $R = \{y \in \mathbb{R} \mid 0 \leq y \leq 4\}$

