

U1D6_T Adding and Subtracting Rational Expressions I

Sunday, February 3, 2019 7:56 PM



U1D6_T
Adding an...

U1D6 MCR 3UI

Adding & Subtracting Rational Expressions Part I

When adding and subtracting rational expressions, we use the same rule for adding and subtracting fractions!

1. Factor ^{the numerator} the denominators(s) (if possible).
2. Determine the common denominator and rewrite the expression with the common denominator.
3. Simplify the numerator(s). (You may need to expand, add/subtract like terms, and then refactor).
4. Divide any common factors if possible.
5. Simplify, if possible.
6. state restrictions on the variable(s).

Examples: Simplify and state restrictions for each of the following.

$$(a) \frac{16t-11}{7} + \frac{4-2t}{7}$$

$$= \frac{16t-11+4-2t}{7}$$

$$= \frac{14t-7}{7}$$

$$= \frac{\cancel{7}(2t-1)}{\cancel{7}}$$

$$= 2t-1$$

* no variable
ever in
denominator
so, no
restrictions.

$$(b) \frac{3m}{8} - \frac{5m}{6} - \frac{2m}{3} \quad \begin{matrix} \times 3 \\ \times 4 \\ \times 8 \end{matrix} \quad \begin{matrix} \text{LCD} \\ 24 \end{matrix}$$

$$= \frac{3m(3)-5m(4)-2m(8)}{24}$$

$$= \frac{9m-20m-16m}{24}$$

$$= \frac{-27m}{24}$$

$$= \frac{-9m}{8}$$

$$\begin{aligned}
 \text{(c)} \quad & \frac{2x}{2x} \frac{3a-b}{9} - \frac{6x}{6x} \frac{a-2b}{3} - \frac{3x}{3x} \frac{4a-3b}{6} \quad \text{LCD } 18 \\
 &= \frac{2(3a-b) - 6(a-2b) - 3(4a-3b)}{18} \\
 &= \frac{6a - 2b - 6a + 12b - 12a + 9b}{18} \\
 &= \frac{-12a + 19b}{18} \quad \text{No restrictions.}
 \end{aligned}$$

$$\begin{aligned}
 \text{(d)} \quad & \frac{2x^2+3x+1}{4x^2-9} - \frac{x^2-3x-1}{9-4x^2} \quad -4x^2+9 \\
 &= \frac{2x^2+3x+1}{4x^2-9} - \frac{x^2-3x-1}{-(4x^2-9)} \times \frac{-1}{-1} \\
 &= \frac{2x^2+3x+1 + (x^2-3x-1)}{4x^2-9}
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{3x^2}{4x^2-9} \quad \text{must factor to find the restriction} \\
 &\quad \text{OR } \frac{3x^2}{(2x-3)(2x+3)} \\
 &\quad 4x^2-9 \neq 0 \\
 &\quad (2x-3)(2x+3) \neq 0 \\
 &\quad 2x-3 \neq 0 \quad \text{or} \quad 2x+3 \neq 0 \\
 &\quad 2x \neq 3 \quad \quad \quad 2x \neq -3 \\
 &\quad x \neq \frac{3}{2} \quad \quad \quad x \neq -\frac{3}{2}
 \end{aligned}$$

$$\begin{aligned}
 4x^2-9 &\neq 0 \\
 4x^2 &\neq 9 \\
 x^2 &\neq \frac{9}{4} \\
 x &\neq \pm \sqrt{\frac{9}{4}} \\
 x &\neq \pm \frac{3}{2}
 \end{aligned}$$

Pgs. 58-59 #1bd, 2acegi, 3ac, 4ac, 5fg, 6ace pg. 60 #11