

U2D1_T- Exponent Laws Part I

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U2D1_T-
Exponent ...

Unit 2: Polynomials (Chapter 3 in Textbook!)

Day 1 - Exponent Laws Part I

A: Simplifying Exponential Expressions -

Product Law

Complete the following table:

Product	Expanded Form	Single Power
a) $(3^2)(3^4)$ <small>$2+4=6$</small>	$3 \cdot 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3$	3^6
b) $(5^3)(5^4)$	$5 \cdot 5 \cdot 5 \cdot 5 \cdot 5 \cdot 5$	5^7
c) $(7^2)(7^4)(7^3)$	$7 \cdot 7 \cdot 7 \cdot 7 \cdot 7 \cdot 7 \cdot 7$	7^9
d) $(x^3)(x^4)$	$x \cdot x \cdot x \cdot x \cdot x \cdot x$	x^7
e) $(x^2)(x^7)(x)$	$x \cdot x \cdot x \cdot x \cdot x \cdot x \cdot x \cdot x \cdot x$	x^{10}

→ or multiplication rule
PRODUCT RULE: When multiplying powers with the same base ... $x^a \cdot x^b = x^{a+b}$

Keep the BASE the SAME
and ADD the EXPONENTS

B: Simplifying Exponential Expressions -
Quotient Law

Complete the following table:

Quotient	Expanded Form	Single Power
a) $(5^3) \div (5^2)$	$\frac{\cancel{5} \cdot \cancel{5} \cdot 5}{\cancel{5} \cdot \cancel{5}} = 5$	$5^1 = 5$
b) $(4^3) \div (4)$	$\frac{4 \cdot \cancel{4} \cdot \cancel{4}}{\cancel{4}} = 4 \cdot 4$	4^2
c) $(3^6) \div (3^4)$	$\frac{\cancel{3} \cdot \cancel{3} \cdot \cancel{3} \cdot \cancel{3} \cdot 3 \cdot 3}{\cancel{3} \cdot \cancel{3} \cdot \cancel{3} \cdot \cancel{3}} = 3 \cdot 3$	3^2
d) $(x^4) \div (x^2)$	$\frac{\cancel{x} \cdot \cancel{x} \cdot x \cdot x}{\cancel{x} \cdot \cancel{x}} = x \cdot x$	x^2
e) $(x^7) \div (x^3)$	$\frac{\cancel{x} \cdot \cancel{x} \cdot \cancel{x} \cdot x \cdot x \cdot x \cdot x}{\cancel{x} \cdot \cancel{x} \cdot \cancel{x}} = x \cdot x \cdot x \cdot x$	x^4

QUOTIENT RULE: When dividing powers with the same base ...
 $x^a \div x^b = x^{a-b}$

Keep the BASE the SAME and
 SUBTRACT the EXPONENTS

Examples: Simplify and evaluate the following:

$$\begin{aligned} \text{a) } & 3^1 \times 3^3 \\ & = 3^{1+3} \\ & = 3^4 = 81 \end{aligned}$$

*ADD exponents
*BASE stays the same

$$\begin{aligned} \text{b) } & 2^2 \times 2^2 \times 2 \\ & = 2^{2+2+1} \\ & = 2^5 = 32 \end{aligned}$$

$$\begin{aligned} \text{c) } & y^2 y^3 y \text{ for (i) } y = 2 \quad \text{(ii) } y = -1 \\ & = y^{2+3+1} \quad \text{(i) } (2)^6 \quad \text{(ii) } (-1)^6 \\ & = y^6 \quad \quad \quad = 64 \quad \quad \quad = 1 \end{aligned}$$

$$\begin{aligned} \text{d) } & 4x^3 x^2 \text{ for } x = 10 \\ & = 4x^5 \quad \quad \quad 4(10)^5 \\ & \quad \quad \quad = 4 \times 100\,000 \\ & \quad \quad \quad = 400\,000 \end{aligned}$$

$$\begin{aligned}
 \text{e) } & 3^5 \div 3^4 \\
 & = 3^{5-4} \\
 & = 3^1 = 3
 \end{aligned}$$

*SUBTRACT EXPONENTS
*BASE stays the same

$$\begin{aligned}
 \text{f) } & 4^6 \div 4^3 \\
 & = 4^{6-3} \\
 & = 4^3 \\
 & = 64
 \end{aligned}$$

$$\begin{aligned}
 \text{g) } & 3x^5 \div x^3 \text{ for } x = 4 \\
 & = 3x^{5-3} \\
 & = 3x^2 \\
 & = 3(4)^2 \\
 & = 3(16) \rightarrow \text{follow BEDMAS} \\
 & = 48
 \end{aligned}$$

$$\begin{aligned}
 \text{h) } & (3m^3n^2)(-m^4n^5) \\
 & = (3)(-1)m^{3+4}n^{2+5} \\
 & = -3m^7n^7
 \end{aligned}$$

$\rightarrow 3, -1$
*multiply the coefficients
*add the exponents on the m's
*add the exponents on the n's

$$i) \frac{-48a^3b^5}{-4ab^2}$$

*divide the coefficients

*subtract the exponents on the a's

*subtract the exponents on the b's

$$= \left(\frac{-48}{-4}\right) \left(\frac{a^3}{a}\right) \left(\frac{b^5}{b^2}\right)$$

$$= 12a^{3-1}b^{5-2}$$

$$= 12a^2b^3$$

$$= \frac{-8m^4n^7}{16n^2}$$

$$= \frac{-1m^4n^5}{2}$$

$$= -\frac{m^4n^5}{2}$$

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(#2 only evaluate b,c,d, #4 only evaluate b,c,d)

NOTE: $a \frac{2}{5} b^3 = \frac{2}{5} ab^3$

+ "Why are Babies Like Hinges..."
see web-page