

Recall:

A quadratic equation:

- Is any equation with a squared variable.
- There is only one variable in the equation.
- To SOLVE it, you need to find the VALUE(S) for the VARIABLE that make(s) the equation true.
- The solutions are called the *roots* of the equation.

To SOLVE a quadratic equation by factoring...

- ✓ Rewrite the equation in standard form (ie. $ax^2 + bx + c = 0$).
- ✓ Factor the quadratic.
3. Solve each factor as a linear equation (ie. Let each factor equal zero and then solve - Lesson 2).
- ✓ These values are your solutions to the quadratic equation.
- ✓ To check, substitute the solution(s) back into the equation and make sure the equation "checks".

Example 1: Solve each of the following by factoring.

a) $x^2 - 2x - 24 = 0$

$(x-6)(x+4) = 0 \quad (2)$

$x-6=0 \quad x+4=0 \quad (3)$

$x=6$

$x=-4$

check: $x=6$

$$\begin{array}{l} \text{L.S.} \\ = (6)^2 - 2(6) - 24 \\ = 0 \end{array} \quad \begin{array}{l} \text{R.S.} \\ = 0 \end{array}$$

check: $x=-4$

$$\begin{array}{l} \text{L.S.} \\ = (-4)^2 - 2(-4) - 24 \\ = 0 \end{array} \quad \begin{array}{l} \text{R.S.} \\ = 0 \end{array}$$

c) $4x^2 + 20x + 25 = 0$

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$(4x+10)(4x+10) = 0$

$2(2x+5)(2x+5) = 0$

$(2x+5)(2x+5) = 0$

Homework: pg. 161 – 162 #1 – 7 (odds for each)

$2x+5=0$

$2x=-5$

$x=-\frac{5}{2}$

$2x+5=0$

$2x=-5$

$x=-\frac{5}{2}$

Check: $x=-\frac{5}{2}$

$$\begin{array}{l|l} \text{L.S.} & \text{R.S.} \\ \hline = 4\left(-\frac{5}{2}\right)^2 + 20\left(-\frac{5}{2}\right) + 25 & = -25 \\ = 4\left(\frac{25}{4}\right) - 50 + 25 & \\ = 25 - 50 + 25 & \\ = -25 & \end{array} \quad \text{L.S.} = \text{R.S.}$$

b) $9x^2 - 25 = 0$

$(3x+5)(3x-5) = 0$

$3x+5=0$

$3x-5=0$

$3x=-5$

$3x=5$

$x=-\frac{5}{3}$

$x=\frac{5}{3}$

d) $2x^2(x+3) = -4x^2(x-1)$

$2x^3 + 6x^2 = -4x^3 + 4x^2$

$2x^3 + 4x^3 + 6x^2 - 4x^2 = 0$

$6x^3 + 2x^2 = 0$

$2x^2(3x+1) = 0$

$2x^2=0$

$x^2=0$

$x=0$

$x=0$

$x=\sqrt{0}$

$x=0$

$3x+1=0$

$3x=-1$

$x=-\frac{1}{3}$