## MHF4UI DETERMINING THE EQUATION OF A GRAPH

Given the graph of a polynomial function and the coordinates of the points on a graph, there are 3 ways to determine the equation:
1)
2)
3)

USING THE ZEROS (AND ONE OTHER POINT)

## Examples

Determine the equation of the following functions.
1.

2.


## DETERMINING AN EQUATION USING REGRESSION

Given the following points determine the equation of the function.

| $X$ | $y$ |
| :--- | :--- |
| 1 | 24 |
| 2 | 12 |
| 3 | 0 |
| 6 | 24 |

Step 1: Add a table to record your data.


Step 3: Add a new equation that is the general form for the function we think this would be (in this case a cubic.... $y=a x^{3}+b x^{2}+c x+d$ ) except use: $x_{1}$ in place of the $x$ so that Desmos knows to use the data we entered in $x_{1}$ in our table) $\sim$ instead of equal sign so Desmos knows it doesn't have to be a perfect fit

a) $(0,2)$, b) $(2,3)$, c) $(3,-5)$, d) $(1,-3 / 2)$

Page 102 \#3ab Finite Differences
Page 102 \#4bcd Regression

## ANSWERS

4. a) $y=1 / 5(x+2)(x-1)(x-5) \quad=1 / 5 x^{3}+4 / 5 x^{2}-7 / 5 x+2$
5. b) $y=-3 / 20 x(x+3)(x-4) \quad=-3 / 20 x^{3}+3 / 20 x^{2}+9 / 5 x$
6. c) $y=5 / 16(x+1)^{2}(x-2)(x-4)=5 / 16 x^{4}-5 / 4 x^{3}-15 / 16 x^{2}+25 / 8 x+5 / 2$
7. d) $y=-3 / 32 x(x+3)(x-2)(x-5)=-3 / 32 x^{4}+3 / 8 x^{3}+33 / 32 x^{2}-45 / 16$
8. a) $y=x^{3}-x+2$
9. b) $y=-x^{3}+4 x^{2}-x-6$
10. b) $y=x^{3}+4 x^{2}-x-3$
11. c) $y=-x^{3}+x^{2}+x+3$
12. d) $y=-x^{4}+5 x^{3}-4$
